# Agent-Based Modeling and Simulation

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#### Credits

- ► These slides are based on the book of Railsback and Grimm [4], chapter 16.
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#### Collectives

- ▶ ABMs represent a system by modeling its individual agents, but surprisingly many systems include intermediate levels of organization between the agents and the system.
- Agents of many kinds organize themselves into collectives, i.e., groups or aggregations of agents that strongly affect both the agents and the overall system.
- Our course of SMA approaches the foundations of these collectives in terms of interaction situations [2] and social actions [1]. The former is quite relevant here.





### Two possible representations

- Emergent. The behavior of the agents allow or encourage them to organize with other agents. The collectives exist only when the agents organize themselves, so that they are given no behaviors or variables of their own.
  - Explicit. The modeler specifies how the collectives, as entities in the ABM, behave and how agents interact with the collectives.





#### **Implementation**

- NetLogo provides breeds: a way to model multiple kinds of turtles or links.
- Breeds let us do many things, including modelling collectives as explicit entities.





### Learning Objectives

- ▶ Learn what collectives are and several ways of modeling them.
- Use NetLogo breeds to represent kinds of turtles.
- ▶ Use NetLogo links to represent relations among turtles of different breeds, which is one way to program collectives.
- Use stochastic modeling by programming and analyzing a new example model of African wild dogs that live in packs.
- ▶ Use logistic functions for representing probabilities and functions that vary nonlinearly between zero and one.





#### Cooperation

- Cooperation among individuals has important advantages, so that systems of all kinds include groups of cooperating individuals.
- ► Example: In biology, cells of different types form organs and other structures to perform functions that the whole organism depends on.
- Example: In many animal and human societies, family and social groups are very important to the behavior, survival, and reproduction of individuals.
- Example: Economic systems contain networks and organizations through which individuals and firms cooperate.





### Explicit modelling

- ► A collective agent typically includes:
  - State variables: especially, a list of the members of the collective; and Sub-models: often including rules for how individuals are added and removed from the collective.
- The individual agents often have:
  - State variable: especially the collectives they belong to; and Sub-models: for how the collective affects them.
- ➤ This approach often adds the least complexity: we can ignore all the individual-level detail that produces the behavior of the collective.

## Representing Collectives via Patches

- ► When the collective is a group of turtles that occupy the same space, it makes sense to represent collectives as patches
- Example: A population of animals or people that live in family or social groups that each occupy a territory (or business, or town).
- ▶ Patch variables can describe the collective's characteristics, e.g., the number of members, perhaps broken out by age, sex, etc.
- ► The primitive turtles—here provides an agentset of member turtles.
- The patch's sub-models could include rules for collective behaviors e.g., adding and removing individuals.



### Representing Collectives via Links

- NetLogo's links might seem natural for modeling collectives because we can think of a collective as a group of individuals that are linked in some way.
- However, NetLogo does not have a built-in way to give variables or rules to a network of linked turtles.
- So links are not easily used to represent collectives with their own behaviors.





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## Using Breeds to Model Multiple Agent Types

- NetLogo provides breeds for modeling different kinds of turtles or links. We discuss only turtle breeds.
- ▶ Breeds are equivalent to subclasses in an OOP language: they let you create several specialized kinds of turtles that have different characteristics from each other, while still sharing some common variables and sub-models.





# Key Points of Using Breeds I

- ▶ Breeds must be defined at the top of the program.
- ► Turtles have a built-in state variable breed. If you create a turtle using create-turtles, its breed variable is set to turtles.
- Using create-<bre>
  <bre>breeds> creates a turtle of the specified breed.
- Example. create-wolves creates a turtle with its value of breed equal to wolves.
- You can change what breed a turtle is by simply using set breed.
- ► Each breed can have its own unique state variables, defined via a <bre>obreeds>-own statement.



## Key Points of Using Breeds II

- ► Each breed still has the built-in variables (xcor, ycor, color, etc.) that NetLogo provides for all turtles.
- ➤ The statement turtles—own can still be used to define variables that all breeds use.
- ▶ If you have defined the breeds wolves and sheep, you can use ask wolves (or sheeps) to have only wolves or only sheep do something. But ask turtles still causes all turtles of all breeds to do something.
- ► Example. Likewise, you can use mean [age] of sheep and mean [age] of turtles to get the average age of just sheep and of all turtles.





# Key Points of Using Breeds III

- Several of the agentset primitives have breed versions.
- ► Example: sheep-here reports an agentset of sheep on a patch, while turtles-here reports all turtles on the patch.
- Breeds do not have their own contexts, all are treated as being in turtle context.
- ► Example. A wolf can try to run a procedure that you wrote for sheep. However, if a wolf tries to use a variable that was defined only for sheep, an error is produced.





#### Similar Breeds

- Although breeds can be very different, e.g., wolves and sheep, this is not necessarily the case.
- They can also represent slight variations of the same agent to analyse the effect of the variation in the same simulation.
- Example: Growers versus savers in an economy, where the only difference between them is the parameter controlling how rapidly they expand.





#### Individuals as Breeds

- Individuals and collectives can be represented as separate breeds, with completely different variables and sub-models.
- ► For this, we must keep track membership:
  - ▶ Each individual has a variable that denotes its collective; and
  - Each collective has a variable that denote their members.
- ► Each time an individual leaves or joins a collective updating is as follows:
  - Individuals are removed/added from/to the collective in question;
  - The individual's variable representing the collective in question must be updated.



### Social Groups

- Some of the clearest examples of collectives are populations of animals that form family or social groups.
- ► These animals typically cooperate within their collectives to obtain food and other resources.
- ▶ However, some behaviors can be tightly regulated within the collectives, e.g., a group's dominant  $\alpha$  male and female mate, but suppress others' reproductive behavior.
- Yet the behavior of the individuals strongly affect their collective, e.g., the reproductive output of the  $\alpha$  couple depends on:
  - How other members decide whether to remain or seek better opportunities elsewhere, and
  - whether individuals leave or die determines the size and structure of the group.



### African Wild Dogs

- ▶ Lycaon pictus are endangered and carefully managed in nature reserves in South Africa [3]. Detailed observations of the wild dogs offer extensive empirical information to use:
  - ► The frequency with which packs produces pups decreases as the total population of dogs increases.
  - Subordinate adults (non  $\alpha$ , two or more years old) often leave their pack as dispersers (the only non- $\alpha$  50% of the time).
  - When two disperser groups of opposite sex and originating from different packs meet, they usually (64% of the time) join to form a new pack.
  - ► The annual mortality rate varies with dog age and is much higher for dispersing dogs than for those in a pack.



#### Structure Of The Model

- ▶ Individual dogs need to be model, since many processes depend on individual variables, e.g., age, sex, and social status.
- ▶ It is clear that no one, but two kinds of collectives are important:
  - Packs
  - Disperser groups
- ▶ Therefore we need three breeds: dogs, packs, and disperser groups.



#### Stochastic Processes

- ► Stochastic sub-models would be very useful.
- ► The behaviors of the dogs and the collectives they form are complex, but frequencies and rates observed in the field can be used as probability parameters for stochastic sub-models.
- ► Reproduction, dispersal decisions, and mortality can all be modeled as stochastic events with probabilities based on observed frequencies.





### Management Actions

- To increase the carrying capacity and therefore the relation between the total number of dogs and the probability of each pack reproducing each year.
- 2. To increase the size of the reserve could reduce the probability that disperser groups encounter each other; and
- 3. Other management actions could reduce the probability that dispersing dogs die before forming a new pack.





#### Purpose

- Evaluating how persistence of a wild dog population depends on:
  - ► The reserve's carrying capacity,
  - The ability of dispersing dogs to find each other, and
  - ► The mortality risk of dispersing dogs.
- Measures of persistence include the average number of years (over a number of replicate simulations) until the population is extinct, and the percentage of simulations in which the population survives for at least 100 years.





#### Usefullness

- ▶ Usefulness of the original model for this purpose is evaluated using five patterns observed in the real wild dog population by Gusset et al. [3].
- ► The patterns relevant to this version of the model include:
  - ► The range (mean and standard error among years) in pack size,
  - Sex ratio,
  - Proportion of the population that are pups, and
  - ▶ Proportion of disperser groups that fail to form new packs.





### Entities, State Variables, and Scales I

- Kinds of agents include dogs, packs, and disperser groups.
- Dogs have state variables for:
  - Age in years,
  - ► Sex.
  - Social status, set as follows:

Status	Age	Observations
pup	0	
yearling	1	
subordinate	$\geq 2$	if it is not an $lpha$ -dog .
alpha	≥ 2	Choosen randomly, one male and one female.
disperser	$\geq 2$	Member of a disperser group, instead of a pack.





### Entities, State Variables, and Scales II

- Dog packs have no state variables.
- ▶ Disperser groups have a state variable for sex (all members are of the same sex) and an identifier of the natal pack of their members.
- Each time step represents one year.
- ► The model is non spatial, locations of packs and dogs are not significant and are only used as visual clues.





### Process Overview and Scheduling I

#### 1. Age and social status update:

- ► The age of all dogs is incremented. Their social status is updated accordingly to their new age (Table, slide 24).
- Each pack updates its  $\alpha$  male and female: If there is no  $\alpha$  of a sex, a subordinate of that sex (if there is one) is randomly chosen.

#### 2. Reproduction:

- If the pack does not include both an  $\alpha$  female and male, no pups are produced, otherwise
- ▶ The probability P of a pack of producing pups depends on the total population at the current time step N, modeled as a logistic function of N, depending on the carrying capacity of the reserve, initially 60 dogs.
- P = 0.5 when N is half of the carrying capacity. P = 0.1 when N is the total carrying capacity.



## Process Overview and Scheduling II

▶ If the pack reproduces, the number of pups is drawn from a Poisson distribution that has a mean birth rate (pups per pack per year) of 7.9. Sex is assigned to each pup randomly, with a 0.55 probability of being male. Pup age is set to 0.

#### 3. Dispersal:

- If a pack has no subordinates, then no disperser group is created.
- ▶ If a pack has only one subordinate of it sex, it has a probability of 0.5 of forming a one-member dispersing group.
- ▶ If a pack has two or more subordinates of the same sex, they always form a disperser group.
- Dogs that join a disperser group no longer belong to their original pack, and their social status is set to disperser.

### Process Overview and Scheduling III

4. Dog mortality is scheduled before pack formation, because mortality of dispersers is high:

Status	Probability
disperser	0.44
yearling	0.25
subordinate	0.20
alfa	0.20
pups	0.12

Mortality of collectives, if any pack or dispersal group has no members, it is removed from the model. If any pack contains only pups, the pups die and the pack is removed.



# Process Overview and Scheduling IV

- 6. Pack formation. Disperser groups that meet other disperser groups of the opposite sex and different original pack, might form a new pack. Each disperser group execute the following steps in random order:
  - Determine how many times the group meets another disperser group, modeled as a Poisson process with the rate of meeting (mean number of times per year that another group is met) equal to the number of other disperser groups times a parameter ( $\geq 1.0$ ) controlling how often groups meet. The following steps are repeated up to rate of meeting times, stopping if the disperser group selects another to join:
    - Randomly select other disperser group. It is possible to select the same other group more than once.



# Process Overview and Scheduling V

- ▶ If the other group is of the same sex, or originated from the same pack, then do nothing more.
- If the other group is of the opposite sex and a different pack, then there is a probability of 0.64 that the two groups join into a new pack. If they do not join, nothing else happens.
- ▶ If two disperser groups do join, a new pack is created immediately and all the dogs in the two groups become its members. The alpha male and female are chosen randomly; all other members are given a social status of "subordinate." The two disperser groups are no longer available to merge with remaining groups.



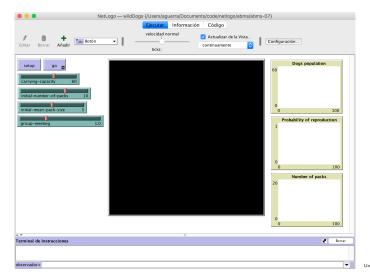


#### Initialization

- ► The model is initialized with 10 packs and no disperser groups.
- ▶ The number of dogs in each initial pack is drawn from a Poisson distribution with mean of 5 (the Poisson distribution is convenient even though its assumptions are not met in this application).
- The sex of each dog is set randomly with equal probabilities.
- ► The age of individuals is drawn from a uniform integer distribution between 0 and 6.
- Social status is set according to age.
- ► The alpha male and female of each pack are selected randomly from among its subordinates; if there are no subordinates of a sex, then the pack has no alpha of that sex.

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#### The exectution tab





#### Global variables

Two global variables are required:

```
globals
[
years-to-simulate ;; set to one houndred by default
prob-reproduction ;; set by a logistic func in the go procedure
]
```



#### **Breeds**

Kinds of agents are implemented as breeds, both individuals (dogs) and collectives (packs and disperser-groups):

```
; Breeds represent collectives and individuals in the model
breed [dogs dog]
breed [packs pack]
breed [disperser-groups disperser-group]
```



#### Other Variables I

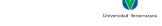
You can define variables for the declared dogs breed:

```
1 | dogs-own
2 | [
3 | age
4 | sex
5 | status
6 | ]
```

As well as disperser groups:

```
d disperser-groups-own
[ [
] sex
[ natal-pack-ID
] ]
```





### Membership to packs and disperser groups

- ► How does a dog know which pack or disperser group it belongs to, and how do packs and groups know which dogs are in them?
- By creating an undirected link between each dog and its pack (or disperser group).
- Packs and disperser groups can refer to their member dogs using the primitive link-neighbors.
- Links are automatically removed whenever the turtle at either end of them dies.
- So a link is added whenever a dog is created or joins a pack or disperser group, a dog can always identify its collective and the collective can always identify its members.

#### Observations

- ► There is one association that links are not useful for: because two disperser groups cannot combine into a new pack if they both originated from the same pack, disperser groups must somehow remember which pack they came from.
- ▶ We could try giving each disperser group a link to the pack that produced it, but if that pack died before the disperser group did, then the link would disappear. Instead, we use the disperser group variable natal-pack-ID to hold the who number of the pack where its members were born.



### Setup

```
to setup
ca
set years-to-simulate 100; number of years to be simulated

create-packs initial-number-of-packs; set at exectuting tab, ten by

default

pack-setup; configure a new pack

pack-setup; configure a new pack

reset-ticks
end
```



## Pack configuration I

```
to pack-setup ; a pack procedure
      ; set a location and shape just for display
      setxy random-xcor random-ycor
      set shape "house"
      set color one-of remove red base-colors
6
      ; create a pack of dogs
7
      let num-dogs random-poisson initial-mean-pack-size
      hatch-dogs num-dogs
10
11
        ; first, set display variables
12
       set shape "dog"
13
14
15
       set heading random 360
       fd 2
16
17
        ; now assign dogs variables
18
       ifelse random-bernoulli 0.5
19
        [set sex "male"]
20
```





## Pack configuration II

```
[set sex "female"]
21
22
        set age random 7
23
24
        set-my-status
25
26
        ; create link between the dog and its pack
        create-link-with myself
27
      ] ; end of hatch-dogs
28
29
30
      ; now select the alpha dogs in the pack
      update-pack-alphas
31
    end ;end of setup-packs
32
```





### Random bernoulli implementation

▶ The random-bernoulli function can be defined as:

```
to-report random-bernoulli [ p ]
report p > random-float 1
end
```



## Updating the status of a dog

```
to set-my-status ; a dog procedure
      (ifelse
       age = 0
         set status "pup"
       ] ; a pup's age is younger than one year
       age = 1
7
         set status "yearling"
         ; a yearling's age is 1
10
        : elsecommands
11
        [if status != "alpha"
12
          [set status "subordinate"]
13
14
15
16
    end ; set-my-status end
```





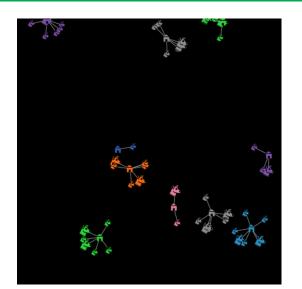
## Updating alphas I

```
to update-pack-alphas; a pack procedure
     let pack-members link-neighbors
     if not any? pack-members with [sex = "female" and status = "alpha"]
       let female-subordinates pack-members with [sex = "female" and status =
            "subordinate"]
       if any? female-subordinates
6
7
         ask one-of female-subordinates
           set status "alpha"
10
           set size 1.5
11
12
13
14
15
        The same for males
16
17
    end ; end update-alphas
18
```



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## Testing the set up





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#### The Schedule I

```
to go
     tick
2
     if ticks >= years-to-simulate [stop]
4
     set prob-reproduction log-func count dogs ; a logistic function of the
6
      ; age and social status update
7
8
     ask dogs
       set age age + 1 ;; dogs become one year older
10
       set-my-status ;; updated accordingly to their age
11
12
13
     ask packs [update-pack-alphas]
14
     ask packs [reproduce]
15
16
     ask packs [disperse]
     ask dogs [do-mortality]
17
     ask packs [do-pack-mortality]
18
     ask disperser-groups [if not any? link-neighbors [die]]
19
```



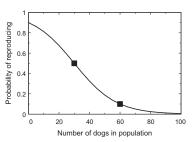
#### The Schedule II

```
ask disperser-groups [do-pack-formation]
20
21
      : Now some defensive programming
22
      ; All dogs should be linked to a pack or disperser group,
23
      ; and all collectives should be linked to dogs.
24
25
      ask turtles with [not any? link-neighbors]
26
27
       error (word "There is a " breed
28
29
         " with no links; who number: " who)
30
      ask turtles with [any? link-neighbors with [breed = [breed] of myself]]
31
32
       error (word breed " " who " is linked to another " breed)
33
34
    end : go ends
35
```



## The logistic function

- They are useful for modeling how the probability of some event depends on one or several variables, because:
  - They produce values in the probability range;
  - They reproduce how probabilities can be very low over a wide range of conditions, very low over a wide range, very high over another range, and change sharply between these two ranges.







### Computation

- Identify two points in the logistic curve:
  - P1 = 30, 0.5, i.e., when the population of dogs is half the capacity of the reserve, the probability of reproduction is 0.5.
  - P2 = 60, 0.1, i.e., when the population of dots equals the capacity of the reserve, the probability of reproduction is 0.1.
- Calculate the following variables:
  - D = ln(P1/(1-P1))
  - C = ln(P2/(1-P2))
  - B = (D C)/(X1 X2)
  - $A = D (B \times X1)$
- ▶ Return P = Z/(1+Z) where  $Z = exp(A + (B \times X))$ .



### Coding the logistic function

```
to-report logFunc [ x ]
      let x1 30
2
      let p1 0.5
      let x2 60
      let p2 0.1
6
      let d ln (p1 / (1 - p1))
      let c ln (p2 / (1 - p2))
      let b (d - c) / (x1 - x2)
      let a (d - (b * x1))
10
11
     let z \exp (a + (b * x))
12
13
     report z / (1 + z)
14
    end ; logFunc ends
15
```





### Testing the function

You can test the function using the command center:

```
Command Center
observer> show logFunc 30
observer: 0.5
observer> show logfunc 60
observer: 0.1000000000000000000
observer> show logfunc 10
observer: 0.812268223212867
observer> show logfunc 5
observer: 0.8618832502903921
observer>
```





### Reproducing I

```
to reproduce ; a pack procedure
     let pack-members link-neighbors
     if count pack-members with [status = "alpha"] = 2; there is a male and
          female alphas
4
       let number-pups random-poisson 7.9 ;; number of born pups
       if random-bernoulli prob-reproduction
         hatch-dogs number-pups
10
           set shape "dog"
11
12
           set age 0 ; new borns are 0 years old
13
14
           set status "pup"
15
16
           ifelse random-bernoulli 0.55; sex is randomly set
           [set sex "male"]
17
           [set sex "female"]
18
19
```



# Reproducing II



### Dispersing

```
to disperse ; a pack procedure
      ; First, identify the subordinates and stop if none
2
     let my-subordinates link-neighbors with [status = "subordinate"]
     if not any? my-subordinates [stop]
      : Now check females
     if count my-subordinates with [sex = "female"] = 1
7
       if random-bernoulli 0.5
8
         create-disperser-group-from my-subordinates with [sex = "female"]
10
11
12
     if count my-subordinates with [sex = "female"] > 1
13
14
       create-disperser-group-from my-subordinates with [sex = "female"]
15
16
      : same for male
17
18
    end ; disperse ends
```

## Dispersing groups I

```
to create-disperser-group-from [some-dogs]; a pack procedure
     hatch-disperser-groups 1; create one disperser group
       set sex [sex] of one-of some-dogs; all members have same sex
       set natal-pack-ID [who] of myself
6
       set shape "car"
7
       set color [color] of myself
       setxy random-xcor random-ycor
       set heading random 360
10
       fd 2
11
12
13
       ask some-dogs
14
15
         ask my-links [die]
         create-link-with myself
16
17
         set status "disperser"
18
         move-to myself
19
         set heading [heading] of myself
20
```





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## Dispersing groups II

```
fd 1 + random-float 2
j ; end of ask some-dogs
j ; end of hatch
end; to create-disperser-group-from
```





### Dogs' death

```
to do-mortality
      (ifelse
2
        status = "disperser"
         if random-bernoulli 0.44 [die]
5
        status = "yearling"
7
8
         if random-bernoulli 0.25 [die]
10
        status = "subordinate" or status = "alpha"
11
12
         if random-bernoulli 0.20 [die]
13
14
          else commands
15
16
         if random-bernoulli 0.12 [die]; pups probability of dying
17
18
19
    end
20
```



#### Packs' death





#### Packs' formation I

```
to do-pack-formation; a disperser-group procedure
     let num-groups-met random-poisson count disperser-groups * group-meeting
     let new-pack-formed false; true if a new pack is formed
     let our-members link-neighbors
     let our-sex sex
     let our-natal-pack-ID natal-pack-ID
7
     repeat num-groups-met
       ask one-of disperser-groups
10
11
         let their-members link-neighbors
12
13
         if sex != our-sex and natal-pack-ID != our-natal-pack-ID
14
15
           if random-bernoulli 0.64
16
17
             set new-pack-formed true
18
             hatch-packs 1
19
20
```

#### Packs' formation II

```
21
                set shape "house"
                set color red
22
23
                setxy random-xcor random-ycor
                let pack-members (turtle-set their-members our-members)
24
25
                ask pack-members
26
27
                 move-to myself
                  set heading random 360
28
                  fd 2
29
                  set status "subordinate"
30
                  ask my-links [die]
31
                  create-link-with myself
32
33
                update-pack-alphas
34
                ; show-pack ; to debug
35
36
              die ; the other disperser-group dies
37
38
39
40
41
```



#### Packs' formation III

```
42 if new-pack-formed [die]; the former disperser-group dies
43 end; do-pack-formation
```

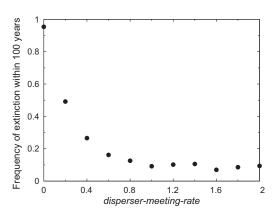




### Dispersers meeting rate effect

- Some reserves have fences to keep dogs from leaving; adding or removing fences could increase or decrease the meeting rate of disperser groups.
- How important is this meeting rate to the persistence of the total dog population?
- Exercise. Do a sensitivity experiment that varies the value of disperser-meeting-rate over a wide range. How frequently the dog population goes extinct in hundred-year simulations: how many times, out of 500 replicate simulations, there are no dogs alive after 100 years.

## Expected plot







#### Observations

- ▶ Increasing the meeting rate above the baseline value (1.0) would not benefit population persistence immensely.
- However, reducing the ability of dispersers to meet is predicted by the model to have stronger negative effects.
- This analysis could indicate to managers that they should avoid actions that make it harder for disperser groups to meet, while not assuming that improving disperser meeting would make the population substantially less likely to go extinct.





### Representations I

- One way to model collectives is as an emergent behavior of the individuals: individuals are modeled in such a way that they can form collectives, and the collectives are strictly an outcome of the model. Example. The butterflies.
- When collectives have important and even moderately complex behavior of themselves, it is typically necessary to model them explicitly as a separate kind of entity with its own state variables and traits.
- ► In NetLogo, one way to model collectives explicitly is to assign the properties and sub-models of collectives to patches.

## Representations II

- ▶ In other models, though, the breeds feature of NetLogo is especially useful for representing collectives because it lets us create multiple kinds of turtles (or links).
- ► Further, NetLogo's links are a simple and relatively reliable way to represent the relations among individuals and their collectives.





#### Cost

- Collectives are often essential in ABMs, but their use has a cost in addition to programming.
- Because collectives are an additional level of organization, we now need to model and analyze how the properties and behavior of collectives and individuals affect each other, as well as how the system affects both collectives and individuals.



#### Referencias I

- C Castelfranchi. "Modelling Social Action for Al Agents". In: Artificial Intelligence 103.1998 (1998), pp. 157–182.
- [2] J Ferber. Les Systèmes Multi-Agents: vers une intelligence collective. Paris, France: InterEditions, 1995.
- [3] M Gusset et al. "Dogs on the catwalk: Modelling re-introduction and traslocation of endangered wild dogs in South Africa". In: *Biological Conservation* 142.2009 (2009), pp. 2774–2781.
- [4] SF Railsback and V Grimm. Agent-Based and Individual-Based Modeling. Second. Princeton, NJ, USA: Princeton University Press, 2019.



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